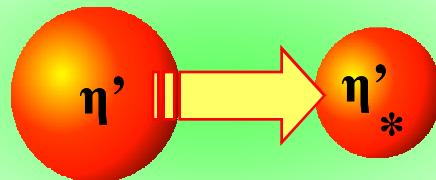


Zimányi '09 Winter School on Heavy Ion Physics



**Significant in-medium reduction
of the mass of η' mesons in
 $\sqrt{s_{NN}} = 200 \text{ GeV Au+Au collisions at RHIC}$**



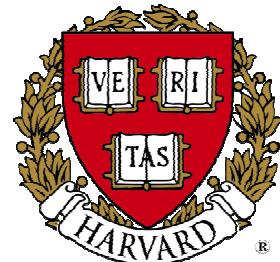
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[arXiv:0912.0258 \[nucl-ex\]](https://arxiv.org/abs/0912.0258)

KFKI Budapest, 12/03/2009

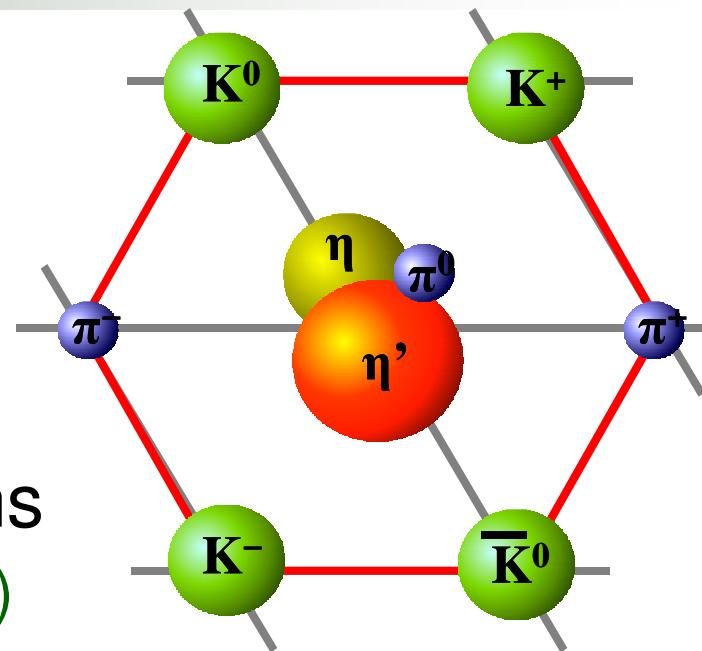


Outline

- **Introduction**
 - Chiral symmetry breaking in the (three-)quark model
 - Symmetry restoration and the η' mass reduction
- **Experimental signatures**
 - Dilepton spectra in Heavy Ion Collisions
 - η' mass through π^\pm Bose-Einstein correlations
 - RHIC vs. SPS
- **Analysis**
 - Simulating the spectra and correlations
 - Fitting the data
 - Systematics
- **Results & conclusion**

Chiral Symmetry Breaking

- The three-quark model
 - SU(3) flavor-symmetry
 - Spontaneously broken
=> 9 Goldstone bosons
 - Corresponding to light mesons
 - There are only 8! (Meson-octet)
- $U_A(1)$ chiral symmetry explicitly broken
 - Distinct topological vacuum-states
 - Tunneling $\leftarrow \rightarrow$ quasiparticles (instantons)
 - 9th boson gains mass – η' (958 MeV)



Restoration of the Symmetry in a Hot, Dense Medium

- High energy densities
 - Strong coupling α_s drops
 - Nontrivial topology vanishes
 - $U_A(1)$ no more broken
 - $SU(3)$ restored

Remark:

From SSB, One expects massless mesons.
However, the flavour symmetry is inexact.

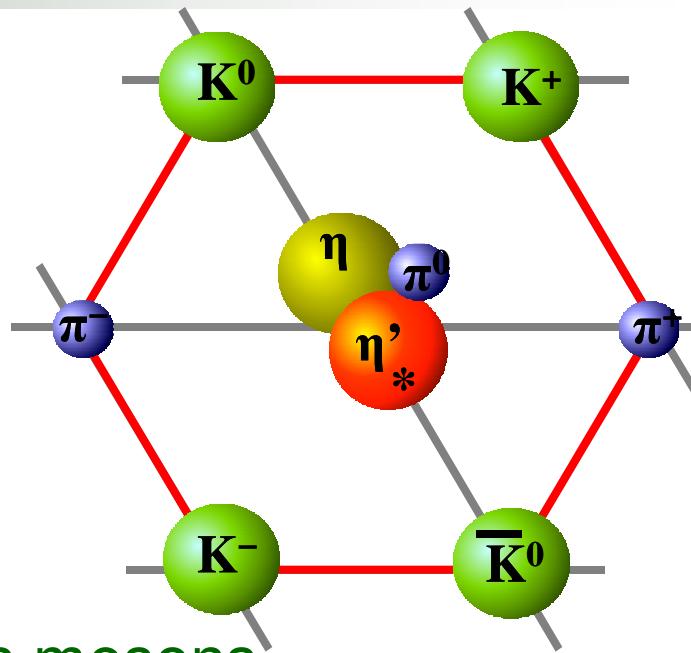
■ Mass reduction

Lower bound (Gell-Mann - Okubo):

$$m_{\eta'}^2 = m_0^2 + \Delta m$$
$$m_0^2 = \frac{1}{3} (2m_K^2 + m_\pi^2); m_0 \approx 400 MeV$$

Upper bound (S,NS isosinglet eigenstate) $m_S^2 = 2m_K^2 + m_\pi^2$; $m_S \approx 700 MeV$

Δm is the extra mass from instantons in a not-so-dense medium



Signature: Particle multiplicity

- Hagedorn-model
 - Production of a light meson
$$\sigma_i \sim (m / 2\pi)^{3/2} e^{-m/T_H} \quad T_H \sim 160 \text{ MeV Hagedorn-temperature}$$
 - Originally, η' mesons are rare: $N_{\eta'} / N_{\pi^0} \sim 2 \times 10^{-2}$
- In case of a possible mass drop:
 - With a strongly reduced η' mass: $N_{\eta'} / N_{\pi^0} \sim 1$
 - An enhancement of a factor of 50 at maximum
 - Increased weight of strange states, rather 3 to 16
- Consequence of the reduced mass:
An increased abundance of η' mesons

The η' through Phase Transition

- Hadronization
 - η' meson production with a reduced mass, thus with an increased multiplicity
- Decoupling from non-Goldstonic matter
 - Mean free path for annihilation is large
 - Long lived
- "Condensate" in the medium
 - Low- p_T η' mesons are unable to get on-shell in the vacuum
 - Medium acts as a trap for low- p_T η' mesons
- As medium dissolves, the η' 's regain their original mass

The Return of the prodigal Goldstone boson. J. I. Kapusta, D. Kharzeev, L. D. McLerran Phys.Rev.D53:5028-5033,1996. arXiv:hep-ph/9507343

Channels of Observation

- Leptonic decay $\eta' \rightarrow \ell^+ \ell^- \gamma$
 - Increased η'/π proportion in the low- p_T range
 - Excess in the $\ell^+ \ell^-$ spectrum under the ρ mass
- η meson (BR=45%) $\eta' \rightarrow \eta \pi^+ \pi^-$
 - Enhancement of η production $\eta \rightarrow \pi^0 \pi^+ \pi^-$
 - BEC of charged pions
 - Sensitive to the sources of the pions
- Direct measurement? $\eta' \rightarrow \gamma \gamma$
 - Would be convincing, however, poor S/B ratio ($\pi^0 \rightarrow \gamma \gamma$)

HBT effect (BEC)

- Discovered and still used in Astrophysics
- Consider two plain waves: $\Psi_1 = e^{-ik_1 x_1}$
 $\Psi_2 = e^{-ik_2 x_2}$
- Bosons: symmetrization needed

$$\Psi_{1,2} = \frac{1}{\sqrt{2}}(e^{-ik_1 x_1} e^{-ik_2 x_2} + e^{-ik_1 x_2} e^{-ik_2 x_1})$$

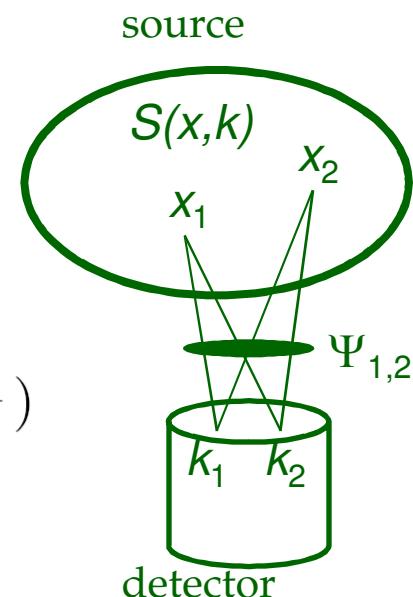
- Spectra: $N_1(k_1) = \int S(x_1, k_1) |\Psi_1|^2 dx_1$
 $N_2(k_1, k_2) = \int S(x_1, k_1) S(x_2, k_2) |\Psi_{1,2}|^2 dx_1 dx_2$

- Correlation:

$$C(k, \Delta K) = \frac{N_2(k_1, k_2)}{N_1(k_1) N_2(k_2)} \quad \Delta K = k_1 - k_2$$

$$k = (k_1 + k_2)/2$$

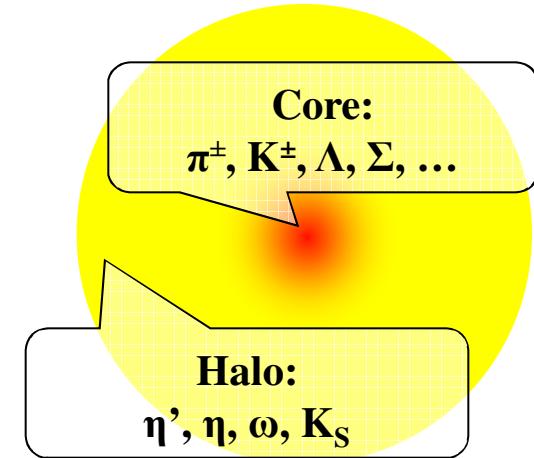
Simplified picture: plain wave, no multiparticle-interactions, thermalization etc.



π^\pm Correlations and the Core-Halo picture

- Pions from QM freezeout

- Primordial (from phase transition)
 - Fast decaying resonances
 - Long-life resonances ($\omega, \eta, \eta', K_S^0$)
- Core Halo



- Correlation

$$C(\Delta k, K) \simeq 1 + \lambda_* R_c(\Delta k, K)$$

$$R_c(\Delta k, K) = \frac{|\tilde{S}_c(\Delta k, K)|^2}{|\tilde{S}_c(\Delta k = 0, K = p)|^2}$$

- Intercept $\lambda_*(m_t) = \left[\frac{N_{core}^{\pi^+}(m_t)}{N_{core}^{\pi^+}(m_t) + N_{halo}^{\pi^+}(m_t)} \right]^2$

$$N_{halo}^{\pi^+} = N_{\omega \rightarrow \pi^+} + N_{\eta \rightarrow \pi^+} + N_{\eta' \rightarrow \pi^+} + N_{K_S^0 \rightarrow \pi^+}$$

$$N = C m_t^\alpha e^{-m_T T_{eff}}, T_{eff} = T_{fo} + m \langle u_T \rangle^2$$

- Correlation measurement $\leftrightarrow \lambda^*(m_T) \leftrightarrow$ core-halo ratio

Simulating the Condensate

- Resonance ratios from different models
ALCOR, FRITIOF, Kaneta *et al.*, Letessier *et. al.*, Stachel *et al.*, UrQMD.
- η' enhancement:
$$\frac{N_{\eta'}}{N_{\eta}} = \left(\frac{m_{\eta'}^*}{m_{\eta}} \right)^\alpha e^{-\left(\frac{m_{\eta'}^* - m_{\eta}}{T_{FO}} \right)}$$
- Restored η' mass: $p_{T,\eta'}^2 + m_{\eta'}^2 = p_{T,\eta}^{*2} + m_{\eta'}^{*2}$
 - If $p_{T,\eta'}^* < \sqrt{m_{\eta'}^2 - m_{\eta'}^{*2}}$, the η' can't get on-shell;
a M-B distribution is assumed:
$$f(p_x, p_y) = \left(\frac{1}{2\pi m_{\eta'} B^{-1}} \right) \exp\left(-\frac{p_x^2 + p_y^2}{2m_{\eta'} B^{-1}} \right) ; \quad p_{T,\eta'}^2 = p_x^2 + p_y^2$$
- Parameters
 - From measurements
 - Conservative assumption
 - Hydrodynamical models expansion)
 - Looked for:
slope B^{-1}

$T_{FO} = 177 \text{ MeV}, \quad \langle u_T \rangle = 0.48$

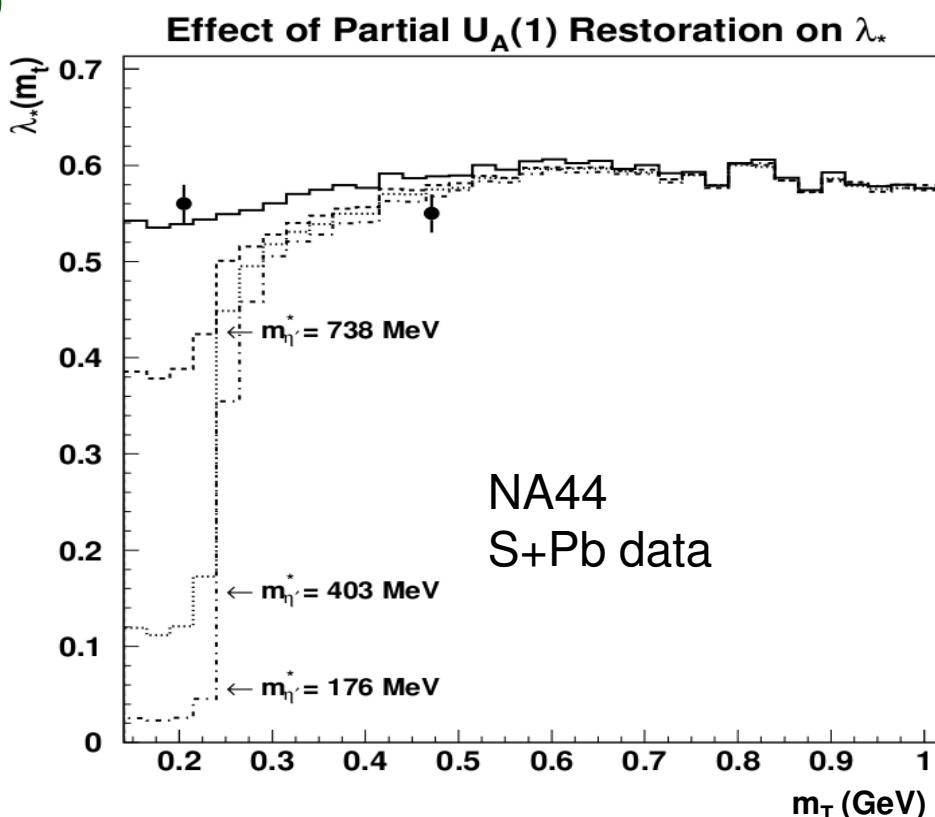
$T_{FO}^{\eta'} = T_{FO} \quad T_{cond} = T_{FO}$

α (related to the dimension of in-medium mass $m_{\eta'}^*$)

inverse

SPS data and simulation: No signal

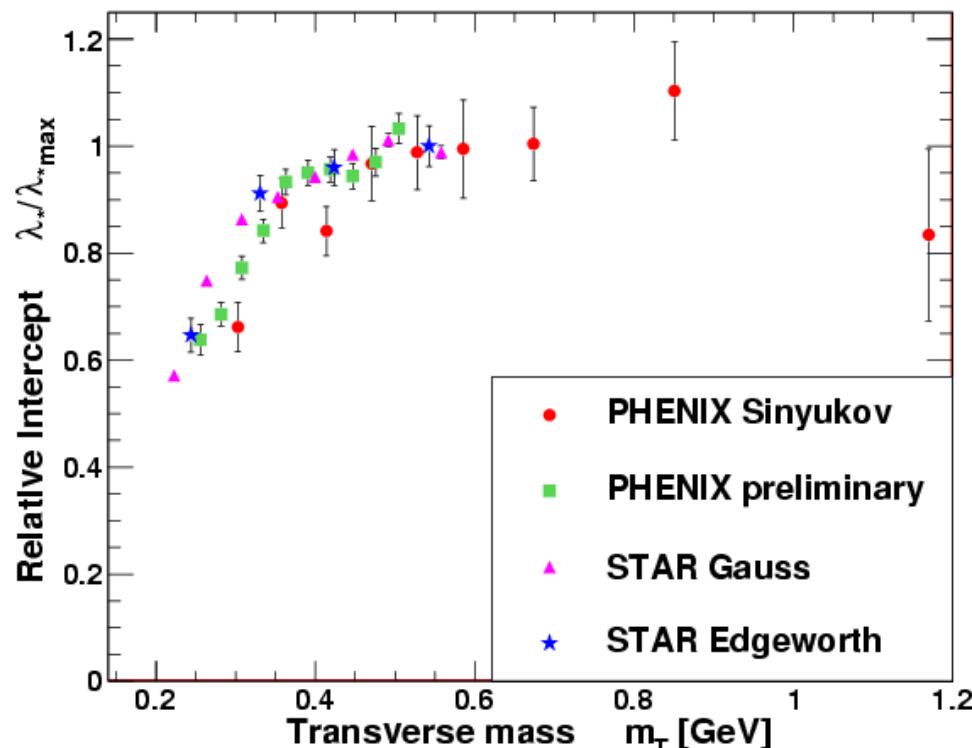
- Data:
NA44 $E_{\text{Lab}}=200 \text{ GeV}$ S+Pb
- Resonances:
FRITIOF
- Earlier, less refined
modeling of condensate
- No sign of mass reduction



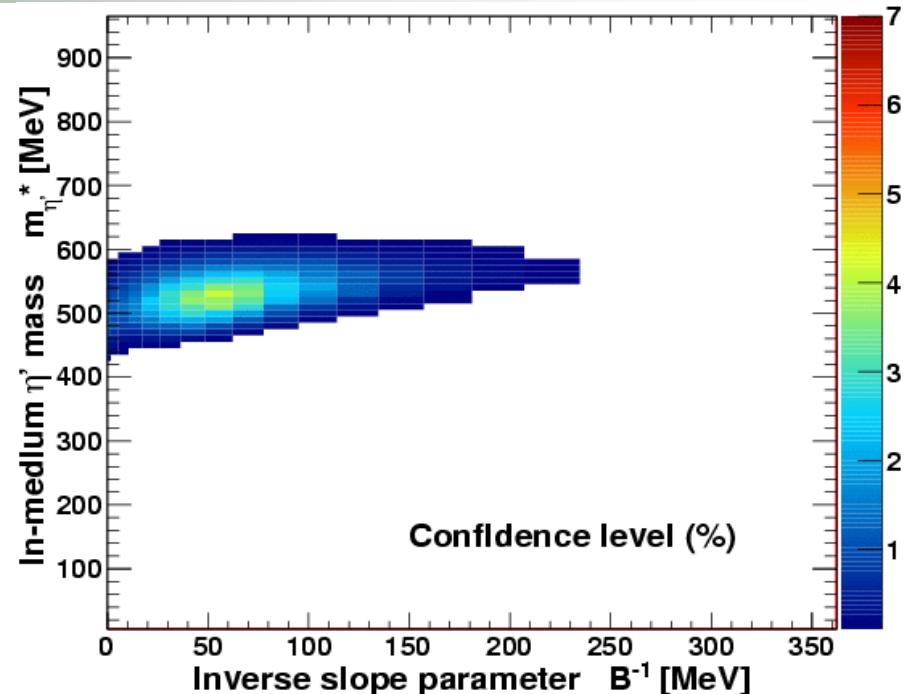
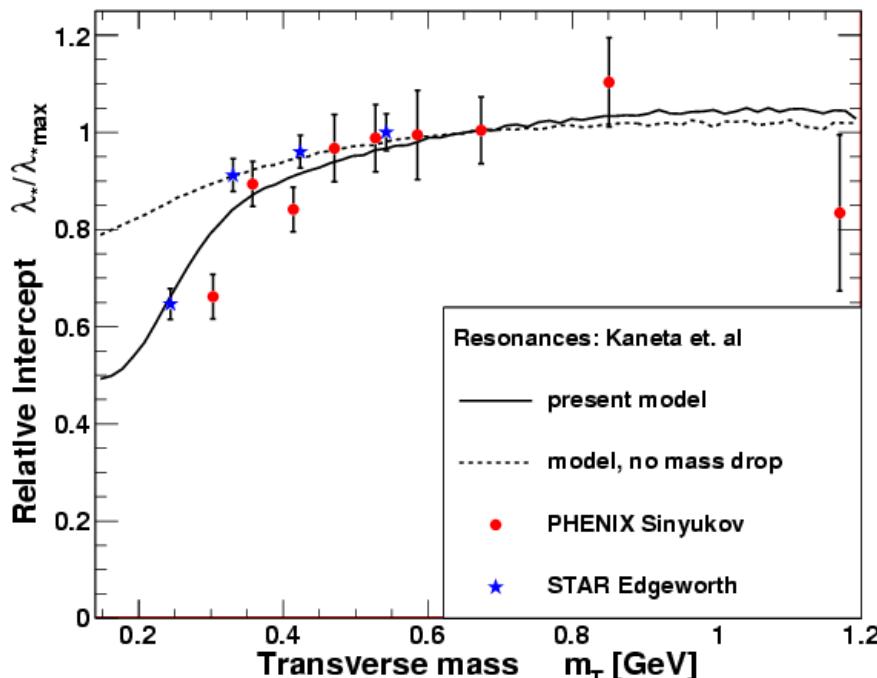
Signal of partial $U(A)(1)$ symmetry restoration from two pion Bose-Einstein correlations
T. Csörgő, D. Kharzeev,, S.E. Vance. e-Print: hep-ph/9910436

RHIC data

- Properties
 - Central Au+Au $\sqrt{s}_{\text{NN}} = 200 \text{ GeV}$
 - Mid-rapidity
PHENIX: $|\eta| < 0.36$ STAR: $|\eta| < 0.50$
 - $\pi^+\pi^+$ correlation measurements
 - $\lambda^*(m_T)/\lambda_{\text{max}}^*$
(different methods)
- Data used in the analysis
 - **PHENIX Sinyukov** 50%
 - **STAR Edgeworth expansion**
(6th order, only even)
- Shown for comparison purposes
 - PHENIX preliminary
 - STAR Gauss

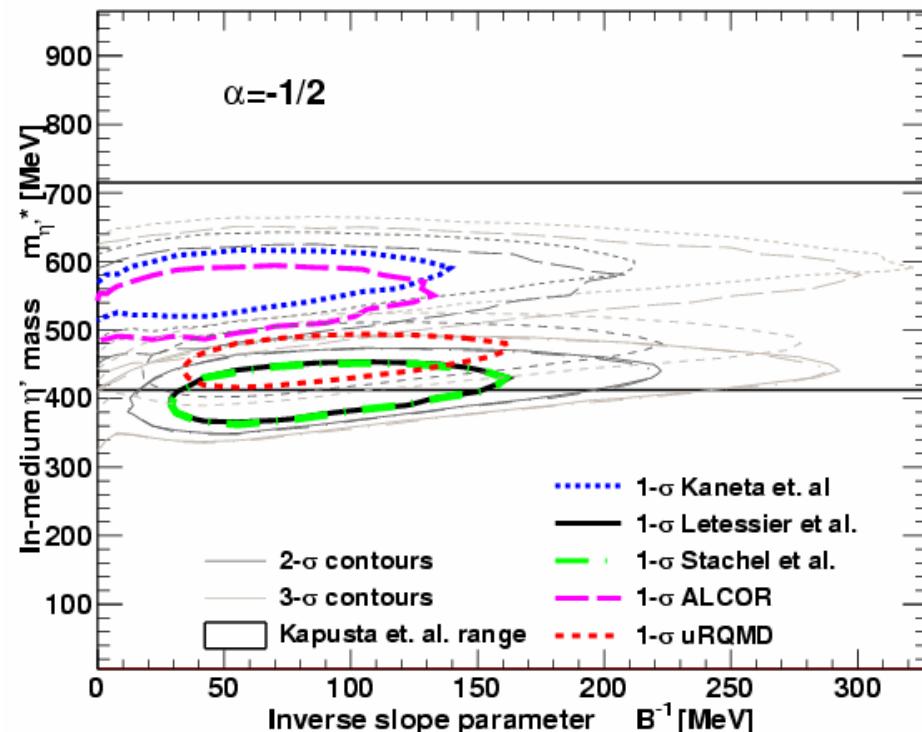
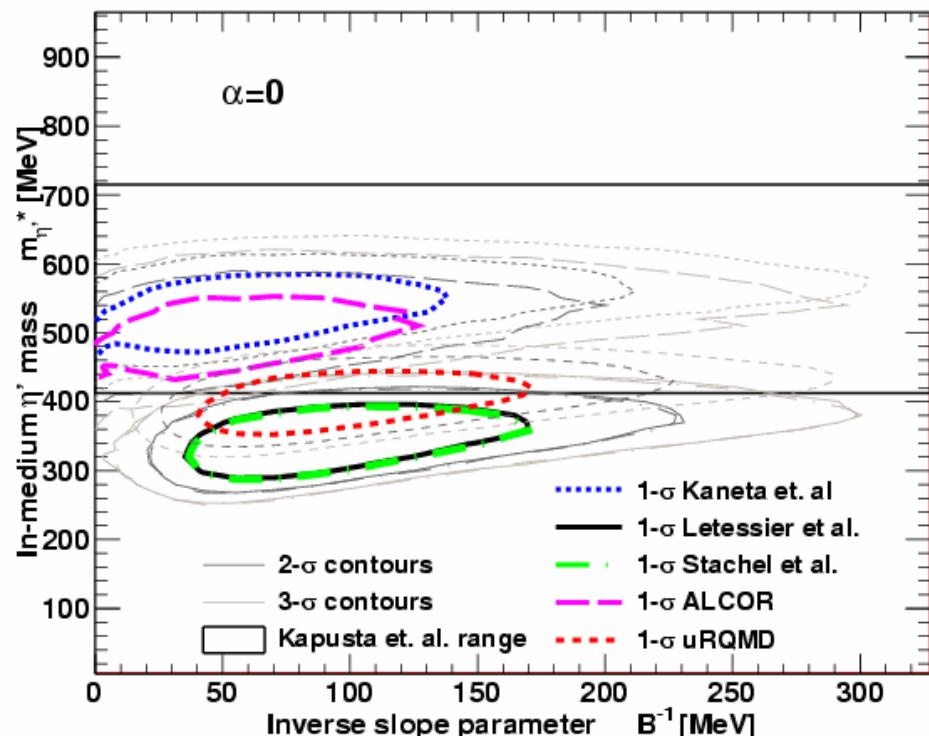


Finding the most likely mass



- Simulations all over the (B^{-1}, m^*) plain
 - Altogether $17 \times 1248 \times 1000000$ events simulated
 - Here: Resonance ratios of **Kaneta & Xu, arXiv:nucl-th/0405068**
- Mapping the confidence level
- Choose best $\lambda^*(m_T)/\lambda_{*,\max}^*$ fit
 - With the shown model: $m_{\eta'}^* = 530$ MeV

Calculations vs. Prediction

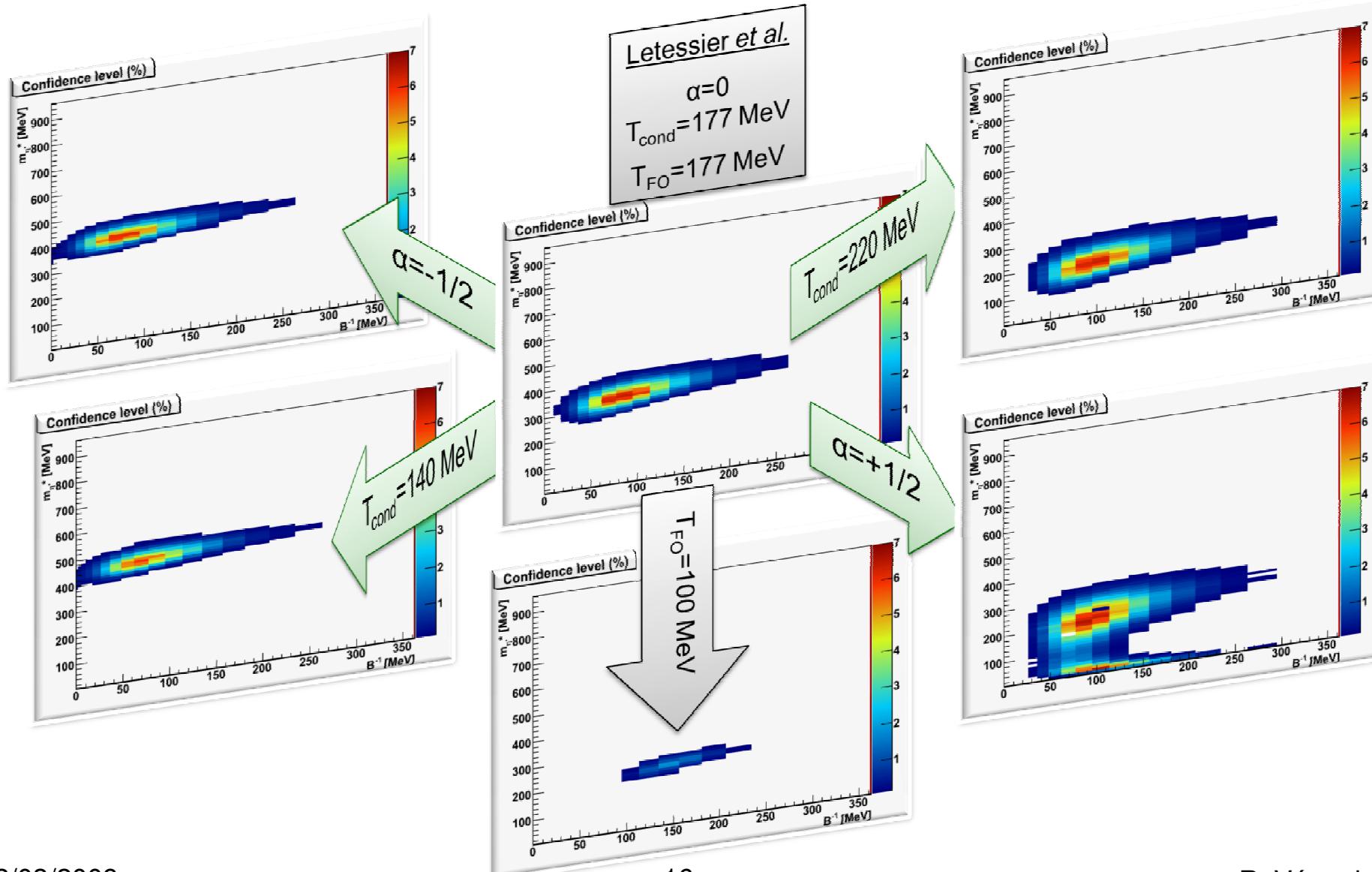


- Theoretical region: [Kapusta et al. arXiv:nucl-th/9507343](#)
- Sigma-contours from model calculations:
either in agreement with theory, or slightly below
- Different α expansion exponents: systematic uncertainty

Systematics and Results

- Systematics
 - Largest uncertainty: models for resonance ratios
 - Modifying parameters in the widest reasonable range
 - $-1/2 \leq \alpha \leq +1/2$ (1)
 - $140 \text{ MeV} \leq T_{cond} \leq 220 \text{ MeV}$
 - $100 \text{ MeV} \leq T_{FO} \leq 177 \text{ MeV}$
 - Other systematics: y -cutoff, core-halo composition
- Best estimate: $m_{\eta'}^* = 340^{+50}_{-60} (\text{stat})^{+280}_{-140} (\text{model}) \pm 30 (\text{syst}) \text{ MeV}$
- An upper boundary can be determined for the η' mass:
No description of data possible when $m_{\eta'}^* > 730 \text{ MeV}$
(An acceptable description means $\text{CL} > 0.1\%$)

Systematics – a Visual Summary



Dilepton Excess in CERES

- Original motivation

Measurement

Model calculations

Excess

in the range b/w the π and ρ mass

- Recently: other explanation

- but...

VOLUME 75, NUMBER 7

PHYSICAL REV

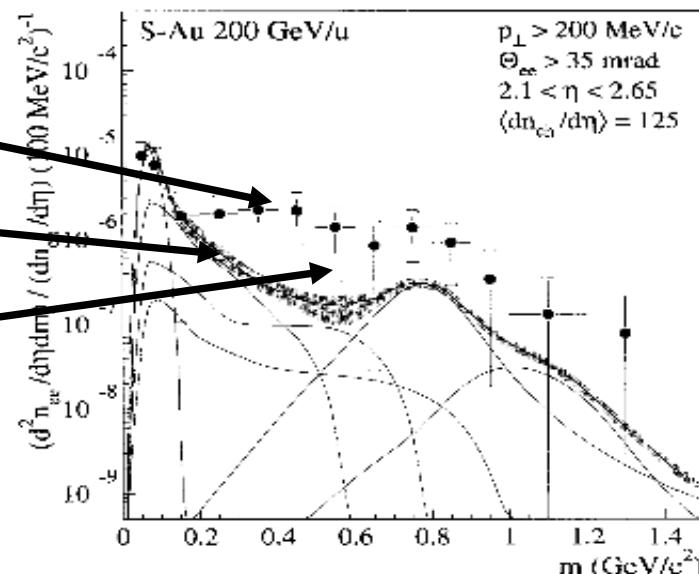


FIG. 4. Inclusive e^+e^- mass spectra in 200 GeV/nucleon S-Au collisions. For explanations see Fig. 2.

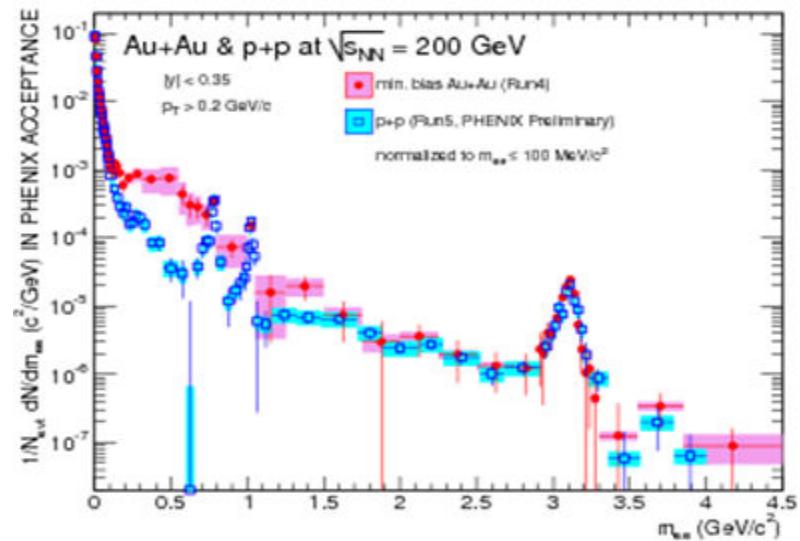
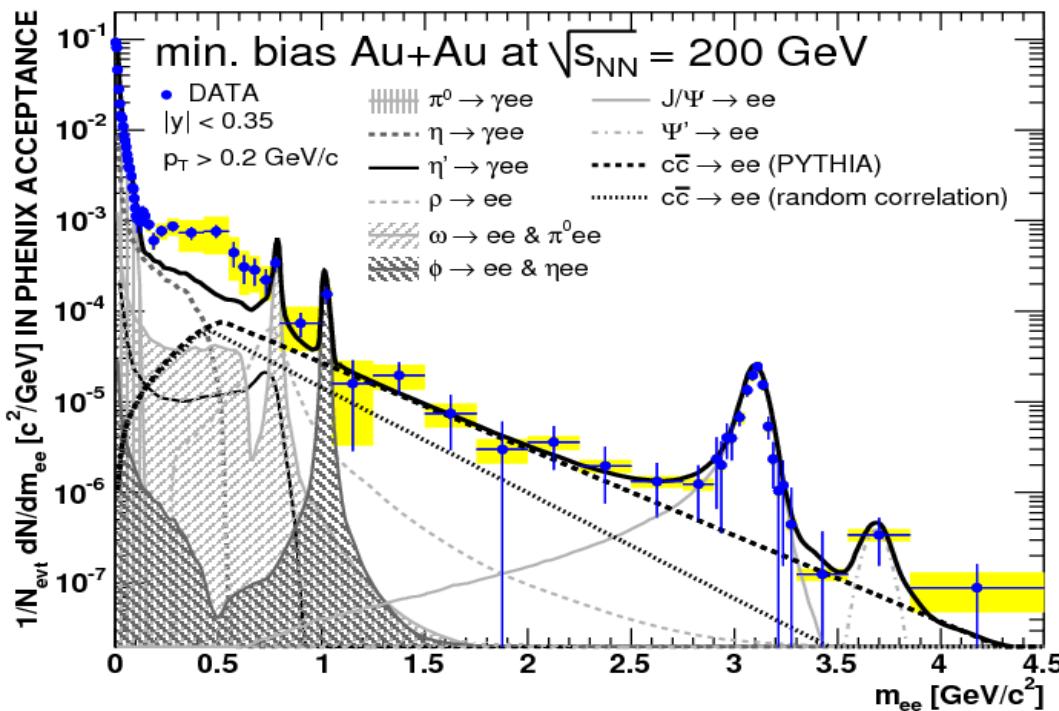
Invariant e^+e^- pair yield measurements compared to hadronic model yields

e^+e^- pair production in Pb - Au collisions at 158-GeV per nucleon.

CERES cn. (G. Agakichiev et al.). Jun 2005. 39pp.

Eur.Phys.J.C41:475-513,2005. e-Print: nucl-ex/0506002

Dilepton Excess in PHENIX



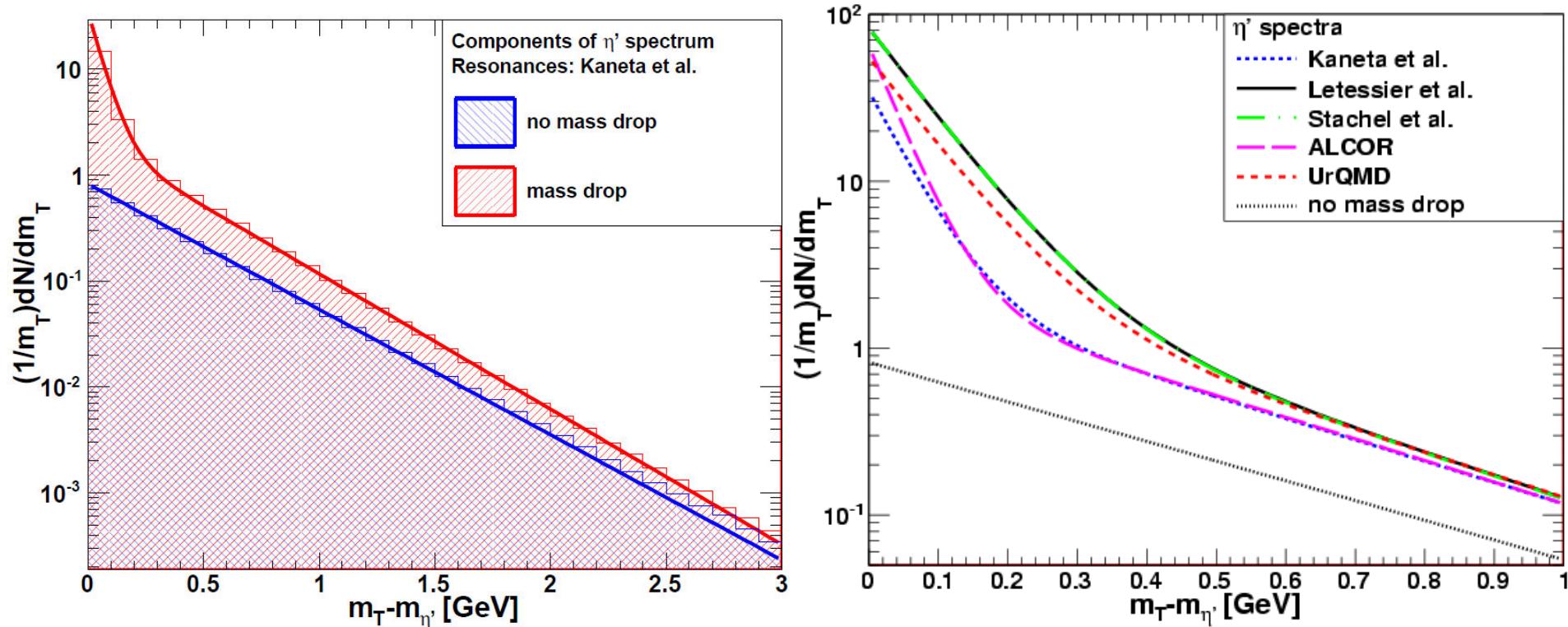
A. Adare *et al.* (PHENIX cn.)
Phys.Lett.B670:313-320,2009.

S. Afanasiev *et al.* (PHENIX cn.)
e-Print: arXiv:0706.3034

Au+Au invariant e+ e- pair yield

- Significant excess in PHENIX 200 GeV Au+Au measurements
- Not present in p+p data – in accordance with hadronic models
- Excess must be an effect of the hot, dense medium

The η' Spectrum



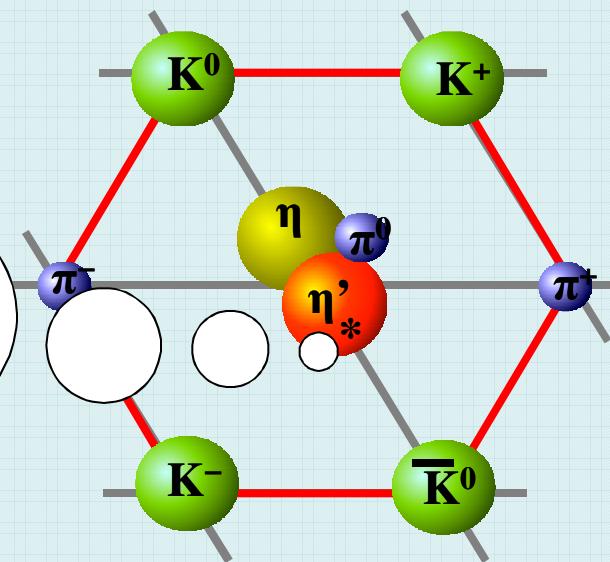
Left: Resonance ratios from **Kaneta – Xu** [arXiv:nucl-th/0405068](https://arxiv.org/abs/nucl-th/0405068)

- An enhancement factor of ~24, mostly at low- p_T
- Breaks m_T – scaling at low- p_T
- Possible explanation of the dilepton excess → needs check!

Conclusion

$m_{\eta^*}^* < m_{\eta} - 220 \text{ MeV}$
at the 99.9% confidence level

from PHENIX+STAR $\pi^+\pi^+$
correlation data + 6 models



- Cross-check with dilepton spectrum needed
- More λ^* data at low p_T is needed to reduce systematics
- Revitalize interest in chiral symmetry restoration

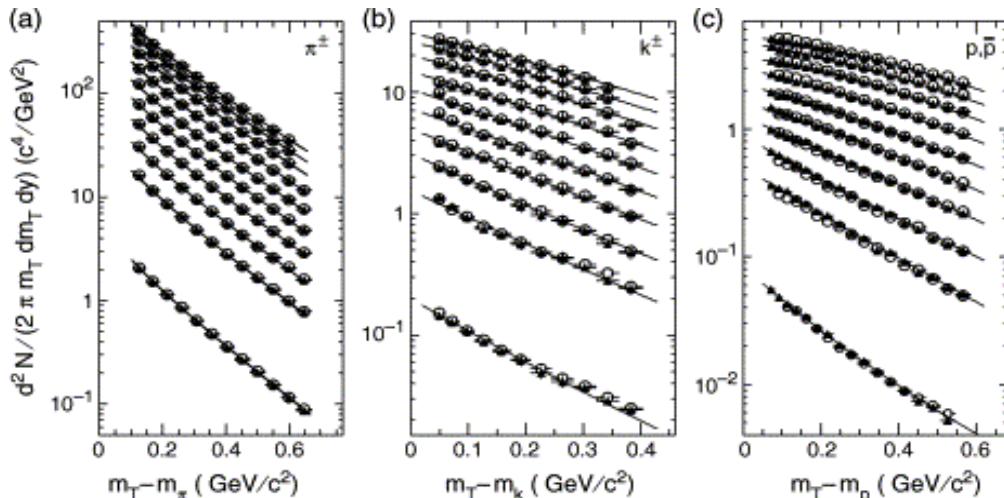
The End



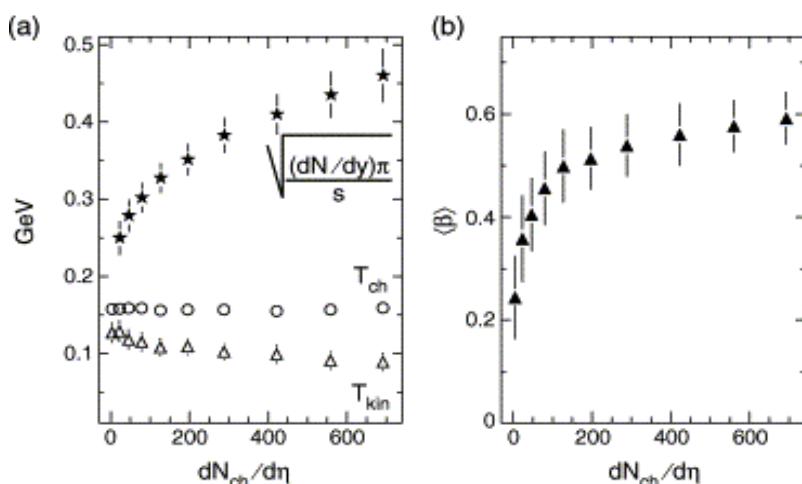
Thank You
for your attention

backup slides follow...

m_T -scaling



central
↑
periph.
pp



$$\frac{dN}{dp_T^2} \sim \exp\left(-\frac{m_T}{T}\right).$$

$$m_t^2 = p_t^2 + m^2$$

E. Shuryak, Prog.Part.Nucl.Phys.53:273-303,2004.

η' mass: Fitted values

	Model Fits for PHENIX+STAR data					Parameters		
	ALCOR	Kaneta <i>et al.</i>	Letessier <i>et al.</i>	Stachel <i>et al.</i>	UrQMD	α	T_{cond}	T_{FO}
$m_{\eta'}^*$ (MeV)	490^{+60}_{-50}	530^{+50}_{-50}	340^{+50}_{-60}	340^{+50}_{-60}	400^{+50}_{-40}	0	177	177
B^{-1} (MeV)	42	55	86	86	86			
CL (%)	4.29	4.12	6.35	6.38	6.28			
$m_{\eta'}^*$ (MeV)	540^{+50}_{-40}	560^{+60}_{-30}	410^{+40}_{-40}	410^{+40}_{-40}	460^{+40}_{-40}	-0.5	177	177
B^{-1} (MeV)	55	55	86	86	86			
CL (%)	2.80	3.35	6.07	5.97	6.14			
$m_{\eta'}^*$ (MeV)			210			+0.5	177	177
B^{-1} (MeV)			86					
CL (%)			6.54					
$m_{\eta'}^*$ (MeV)		620	460			0	140	177
B^{-1} (MeV)		42	69					
CL (%)		2.26	5.86					
$m_{\eta'}^*$ (MeV)		440	200			0	220	177
B^{-1} (MeV)		69	104					
CL (%)		5.61	6.33					
$m_{\eta'}^*$ (MeV)		410	240			0	177	100
B^{-1} (MeV)		145	145					
CL (%)		1.63	1.80					

TABLE II: Fitted values of the modified η' mass on the STAR+PHENIX combined dataset, for different resonance models and parameters. The Fritiof model has CL< 0.1% and therefore not shown here. 1- σ boundaries of the fits are given only for $m_{\eta'}^*$ and for the $\alpha = 0$ and $\alpha = -0.5$ simulations, not for all the systematic checks.

η' mass: Acceptability boundaries

Dataset	Acceptability boundaries of model fits						Parameters		
	ALCOR	FRITIOF	Kaneta <i>et al.</i>	Letessier <i>et al.</i>	Stachel <i>et al.</i>	UrQMD	α	T_{cond}	T_{FO}
PHENIX	0—750	680—958	0—720	0—510	0—500	0—530			
STAR	380—600	none	430—630	190—450	190—450	260—500	0	177	177
PHENIX+STAR	380—590	none	420—620	260—430	260—430	330—470			
PHENIX	30—770	420—958	50—730	0—540	0—540	0—560			
STAR	470—630	none	500—650	300—500	300—500	360—540	-0.5	177	177
PHENIX+STAR	450—620	670—760	490—640	340—480	340—480	400—510			
PHENIX				0—450					
STAR				0—390			+0.5	177	177
PHENIX+STAR				0—390					
PHENIX			0—760	0—450					
STAR			560—690	0—390			0	140	177
PHENIX+STAR			540—680	0—360					
PHENIX			0—680	0—410					
STAR			270—580	0—350			0	220	177
PHENIX+STAR			290—560	100—320					
PHENIX			220—470	30—310					
STAR			360—470	190—300			0	177	100
PHENIX+STAR			370—440	200—280					

TABLE III: Acceptability boundaries of the modified η' mass on the PHENIX, STAR, and the STAR+PHENIX combined datasets, for different resonance models and parameters. A fit is considered acceptable if $CL \geq 0.1\%$. There is no model and no sane set of parameters that contradict with an $m_{\eta'}^* \leq 760$ MeV assumption for the combined PHENIX+STAR dataset. However, all the models except for the FRITIOF, the one that completely fails on the STAR dataset, require an $m_{\eta'}^* \leq 640$ MeV.

Dilepton excess in details

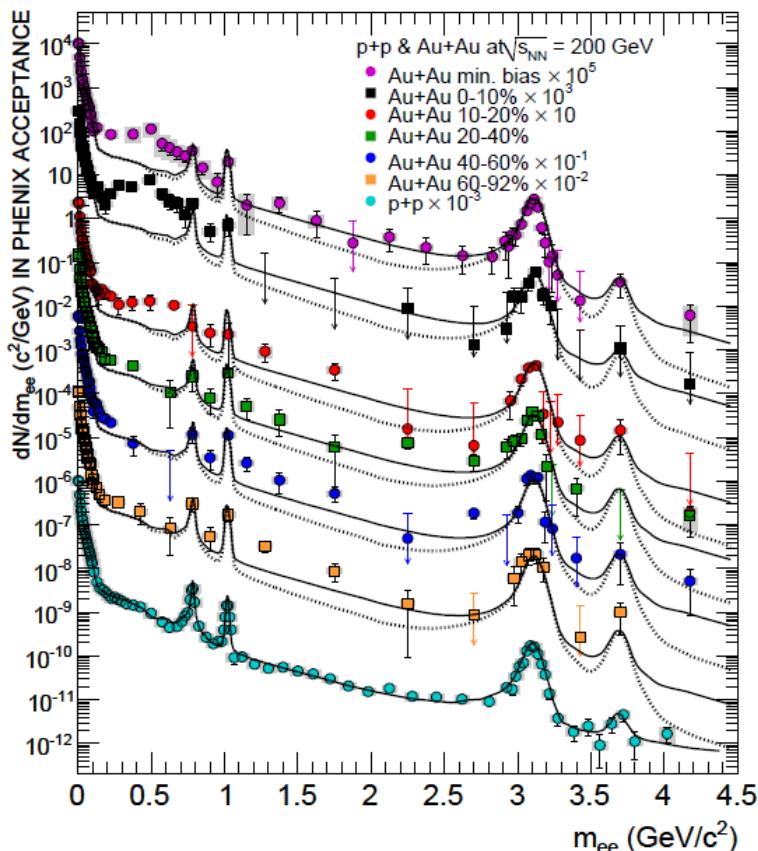


Fig.26: Invariant mass spectrum of e^+e^- pairs compared to expectations from the model of hadron decays for $p+p$ and for different $Au+Au$ centrality classes.

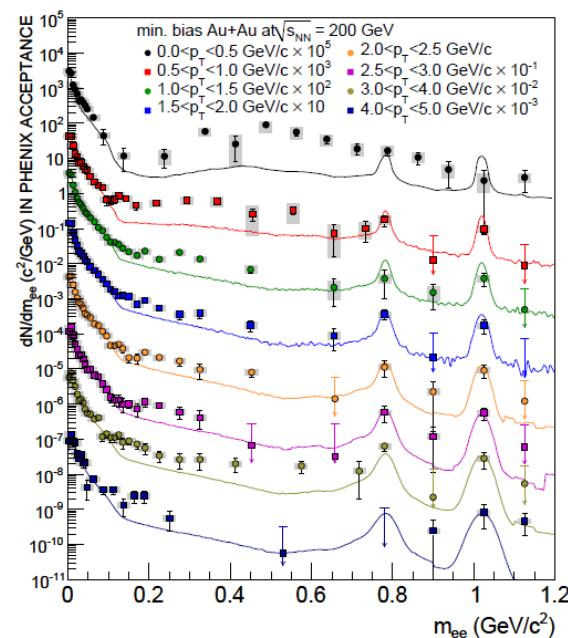
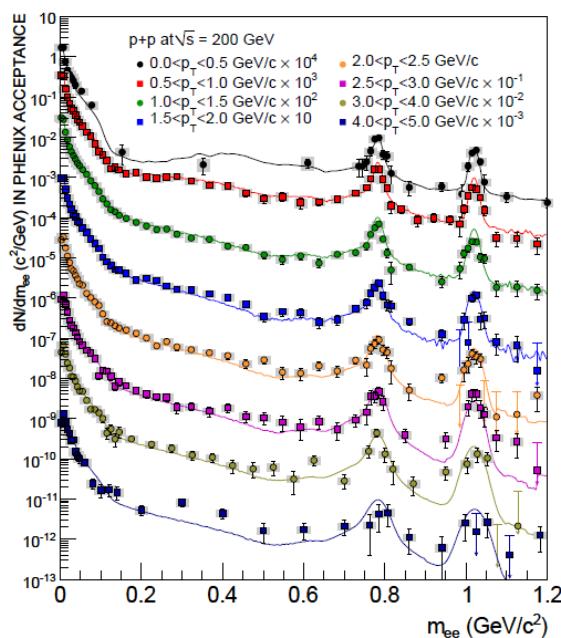
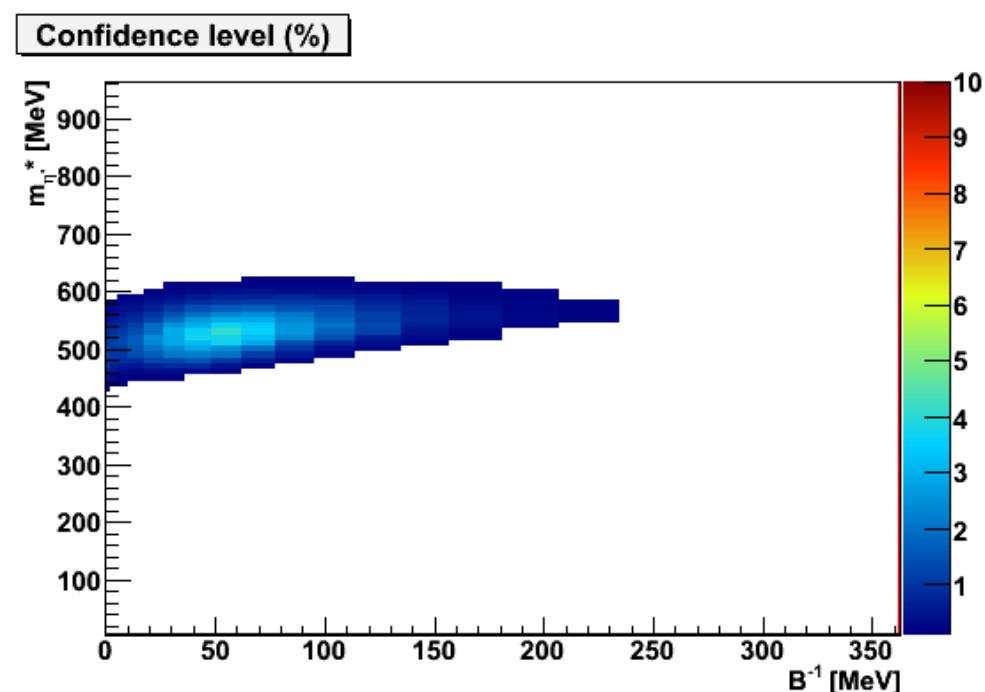
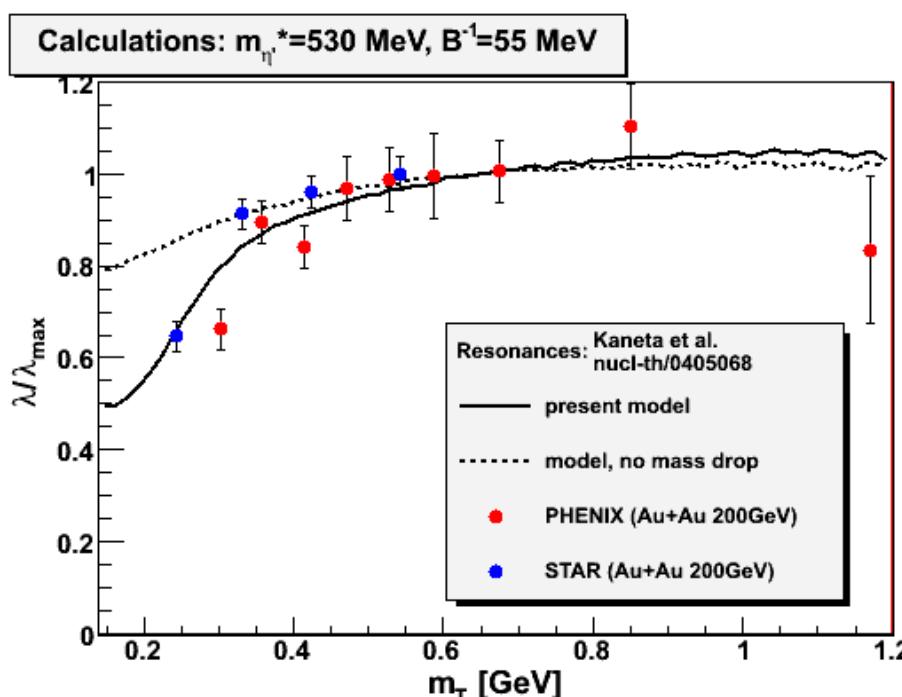


Fig.29: e^+e^- pair invariant mass distributions in $p + p$ (left) and minimum bias $Au+Au$ collisions (right). The p_T ranges are shown in the legend.

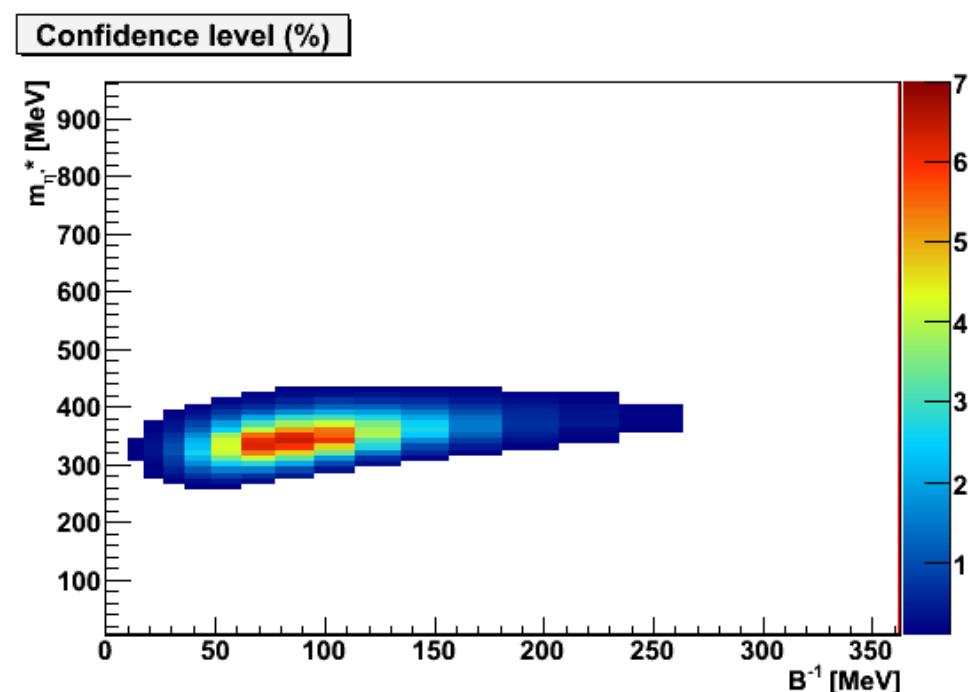
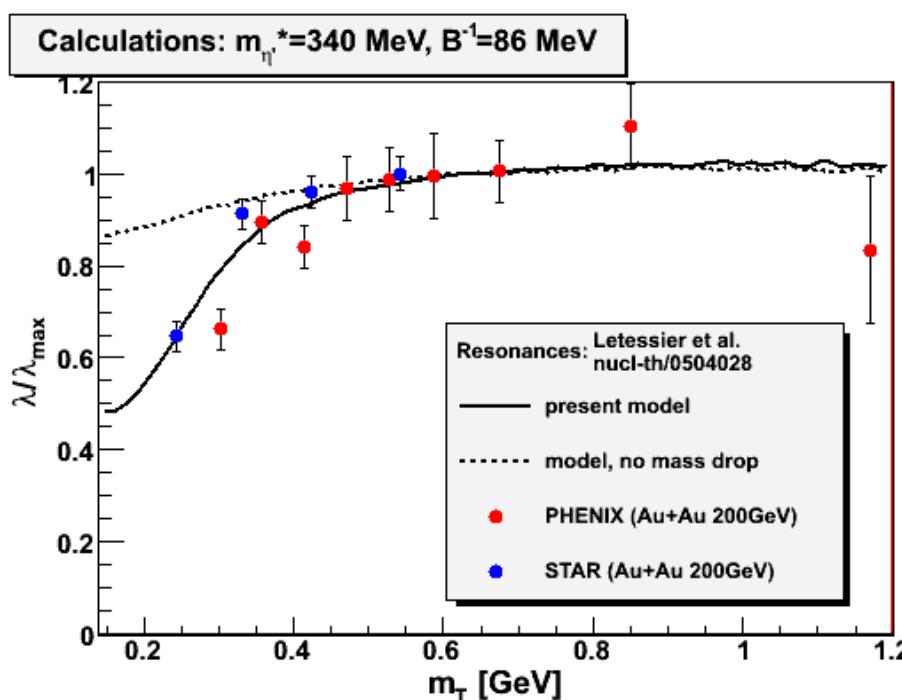
Resonances: Kaneta-Xu vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au
- Describes PHENIX hadron spectrum well

Kaneta & Xu, arXiv:nucl-th/0405068

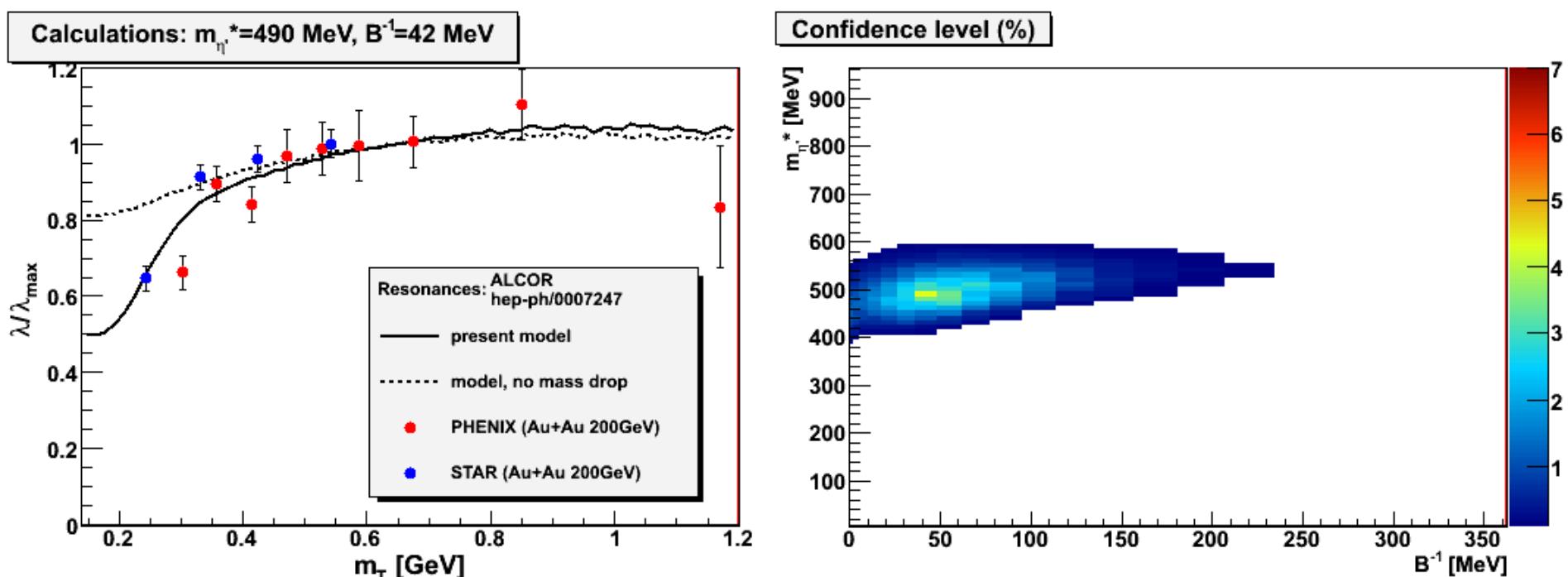
Resonances: Letessier-Rafelski vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au

J.Letessier J.Rafelski, arXiv:nucl-th/0504028

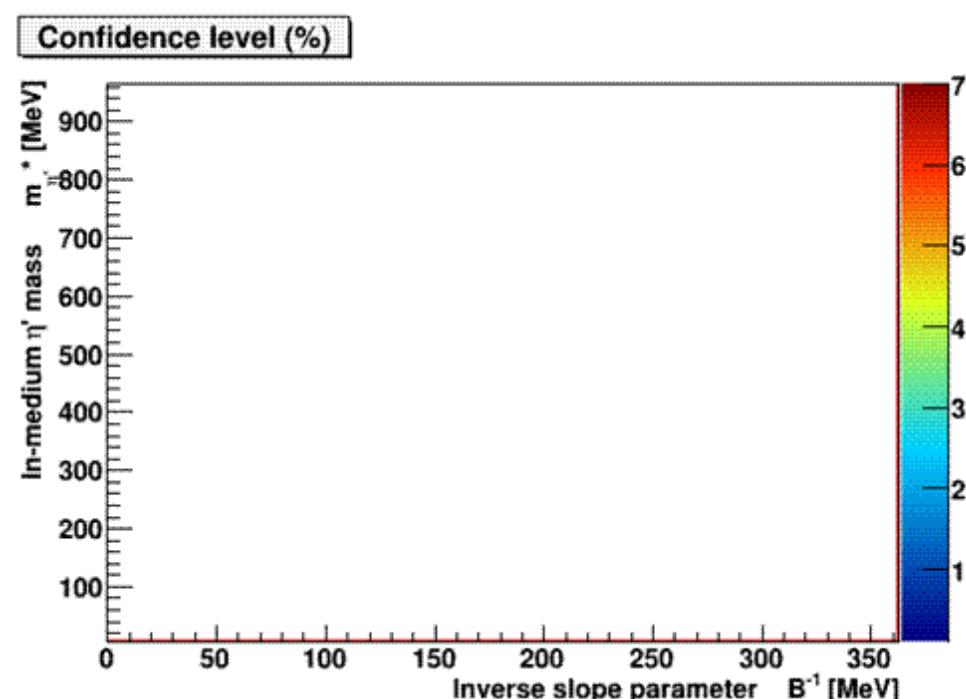
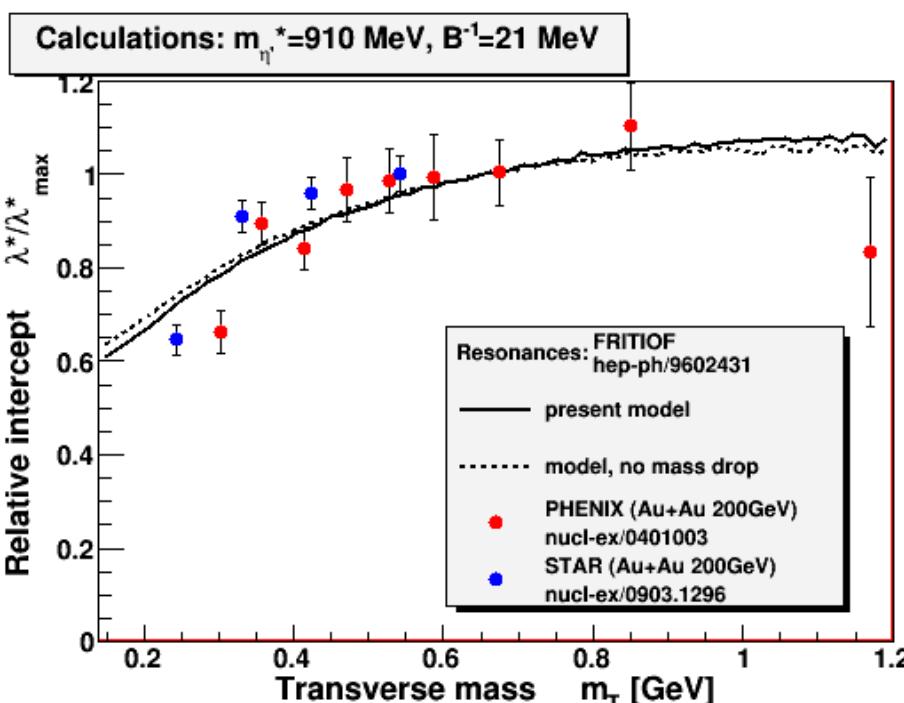
Resonances: ALCOR vs. RHIC



- Coalescence-model
- η'/η ratio has to be fixed from other models
(Kaneta, here)

P. Levai, T.S. Biro, T. Csorgo, J. Zimanyi, hep-ph/0007247

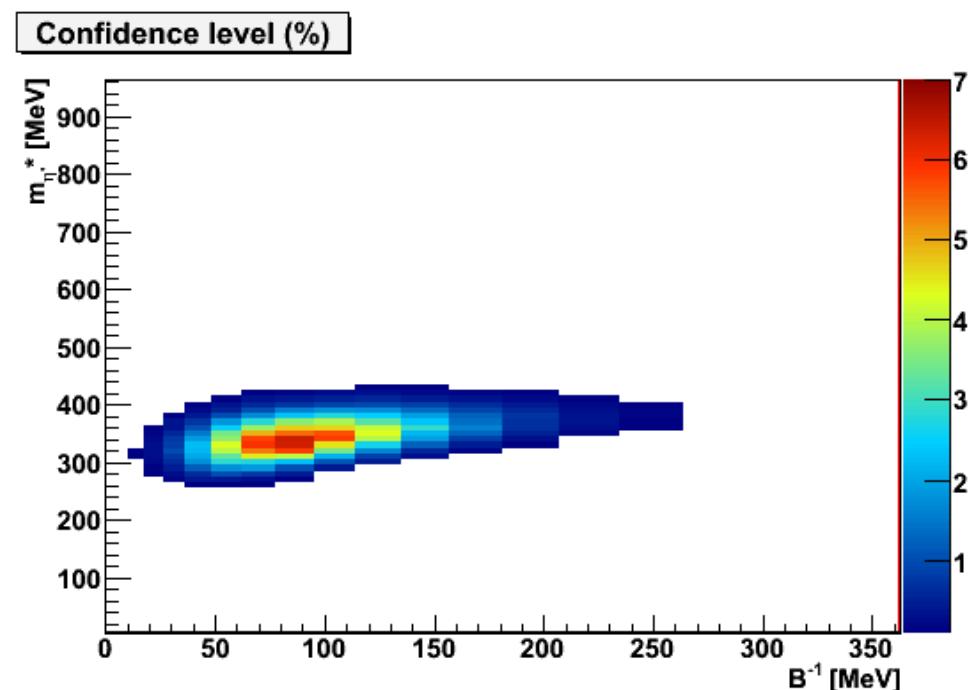
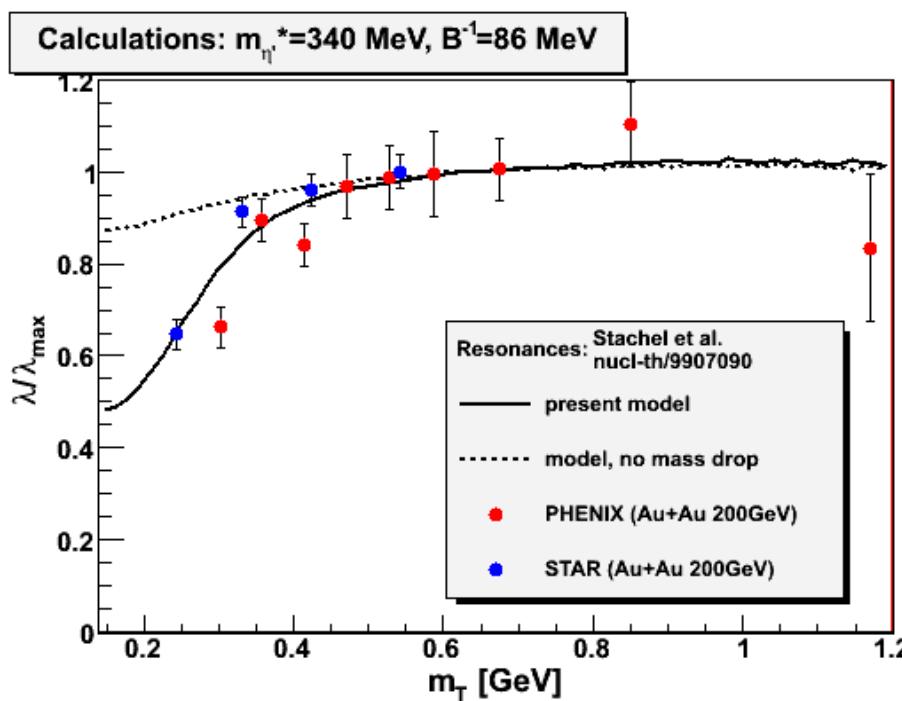
Resonances: FRITIOF vs. RHIC



- 200 GeV mid-rapidity Au+Au simulation
- Note: Does not describe STAR data, neither the unified PHENIX+STAR dataset. For PHENIX data only, it is consistent with $m_{\eta^*} = 958 \text{ MeV}$.

B. Anderson et al., Nucl. Phys. B 281 (1987) 289.

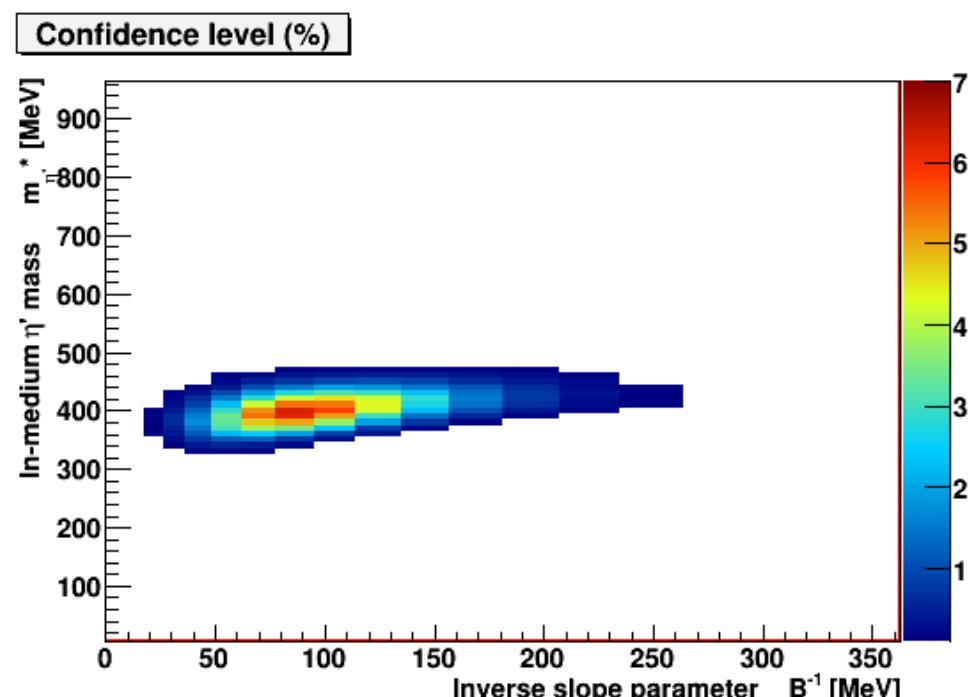
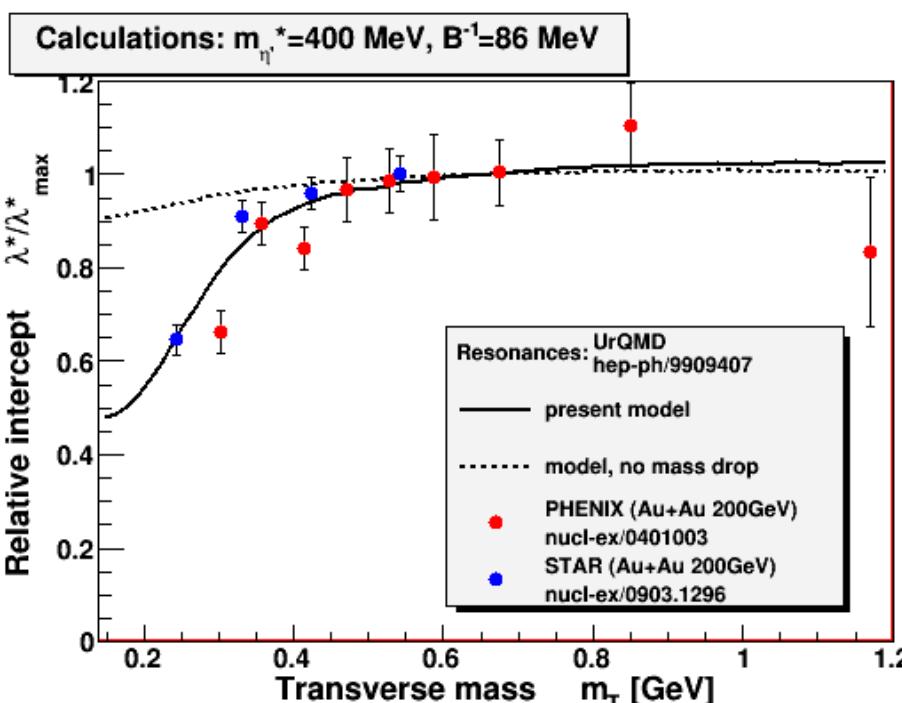
Resonances: Stachel et al. vs. RHIC



- Statistical chemical freezeout model
- Central mid- η 200 GeV Au+Au

J.Stachel et al., arXiv:nucl-th/9907090

Resonances: UrQMD vs. RHIC

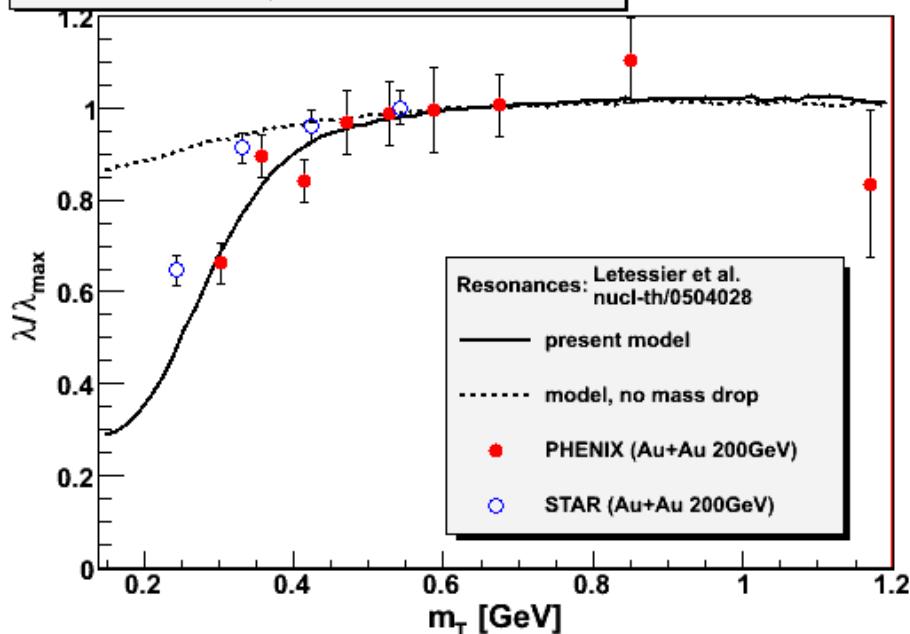


- 200 GeV midrapidity
- Au+Au, RHIC $\sqrt{s}_{NN} = 200 \text{ GeV}$

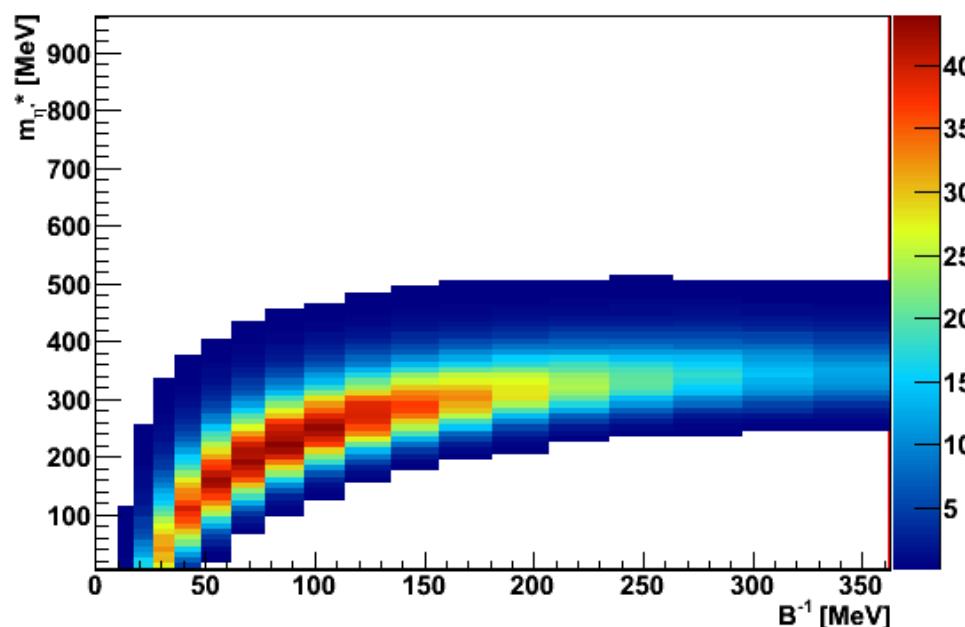
J. P. Sullivan et al., Phys. Rev. Lett. 70 (1993) 3000

Rafelski vs. PHENIX

Calculations: $m_{\eta^*}=220$ MeV, $B^{-1}=86$ MeV

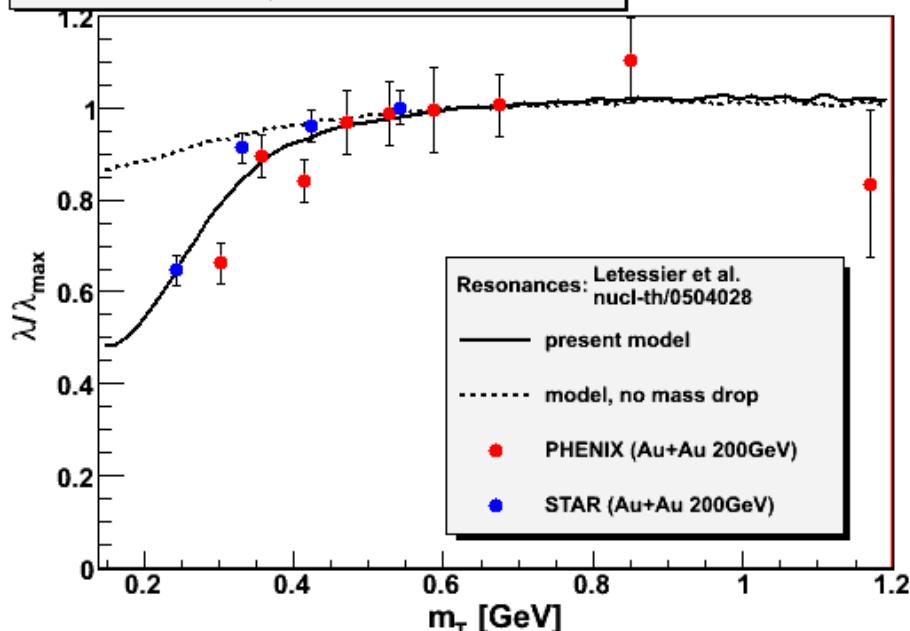


Confidence level (%)

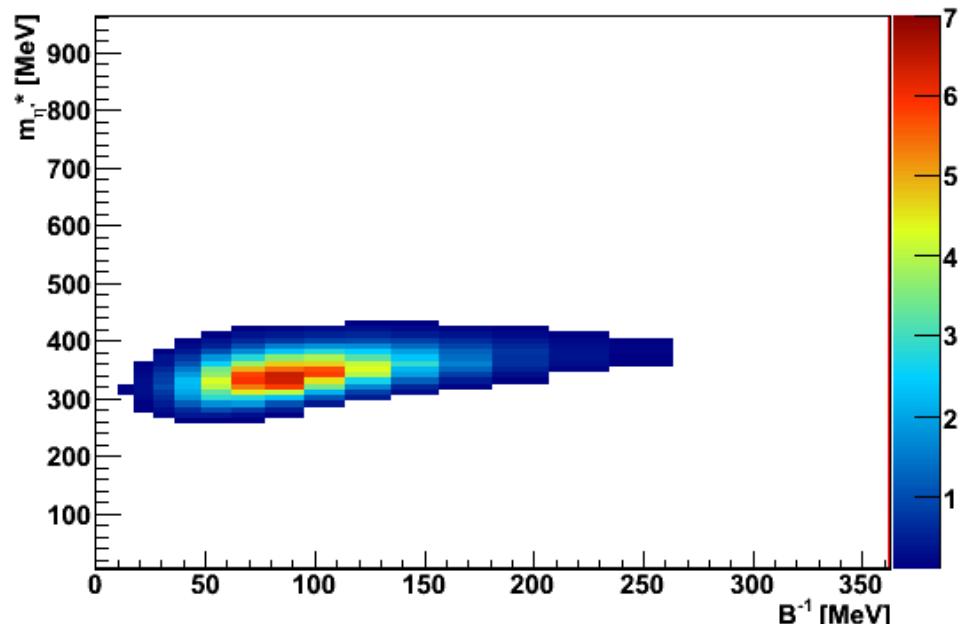


Rafelski vs. PHENIX & STAR

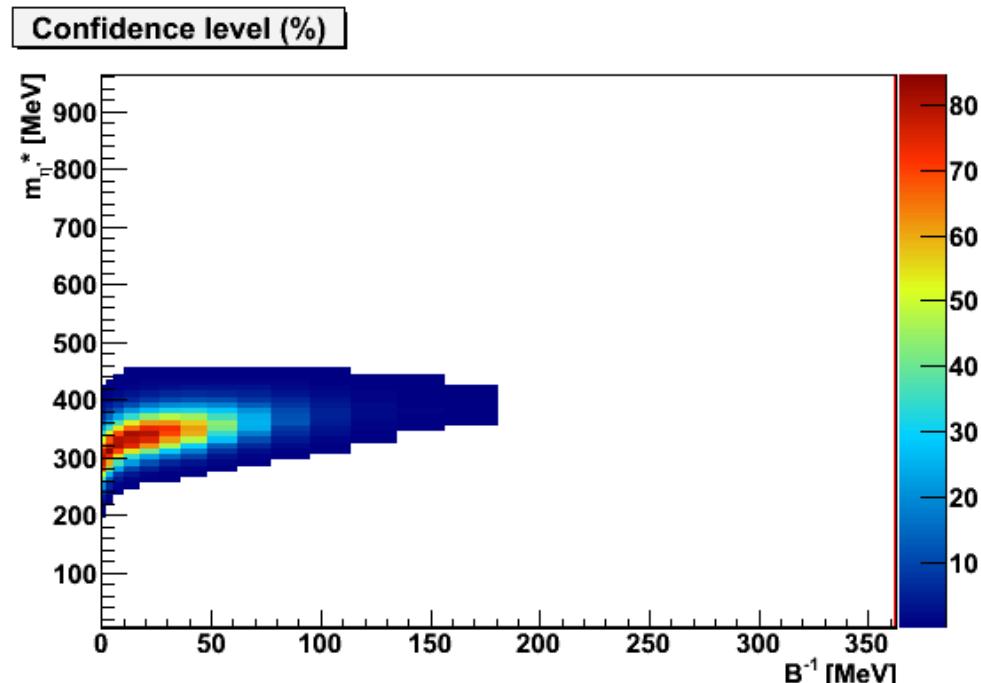
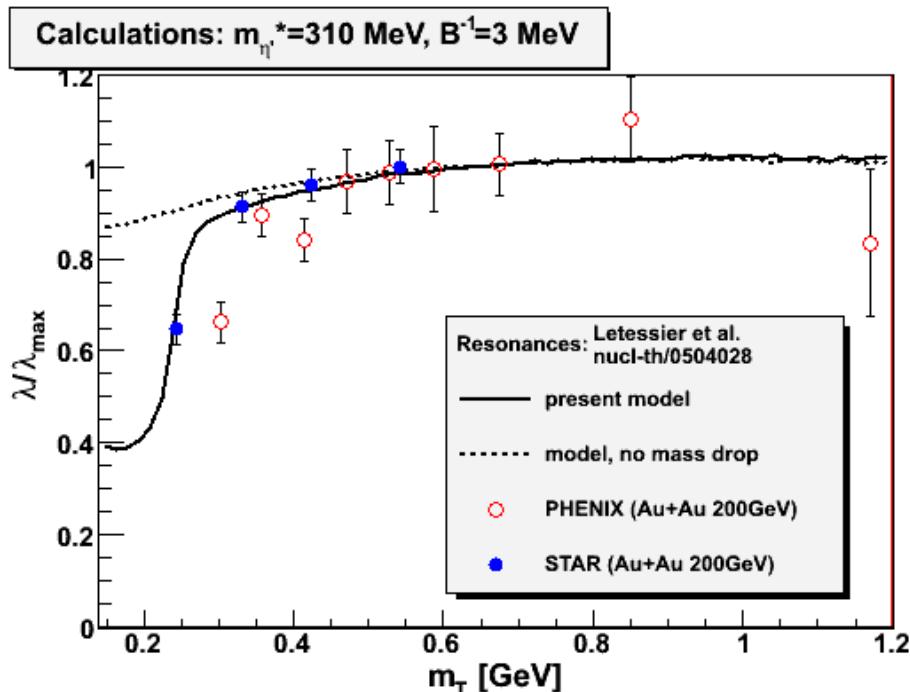
Calculations: $m_{\eta^*}=340$ MeV, $B^{-1}=86$ MeV



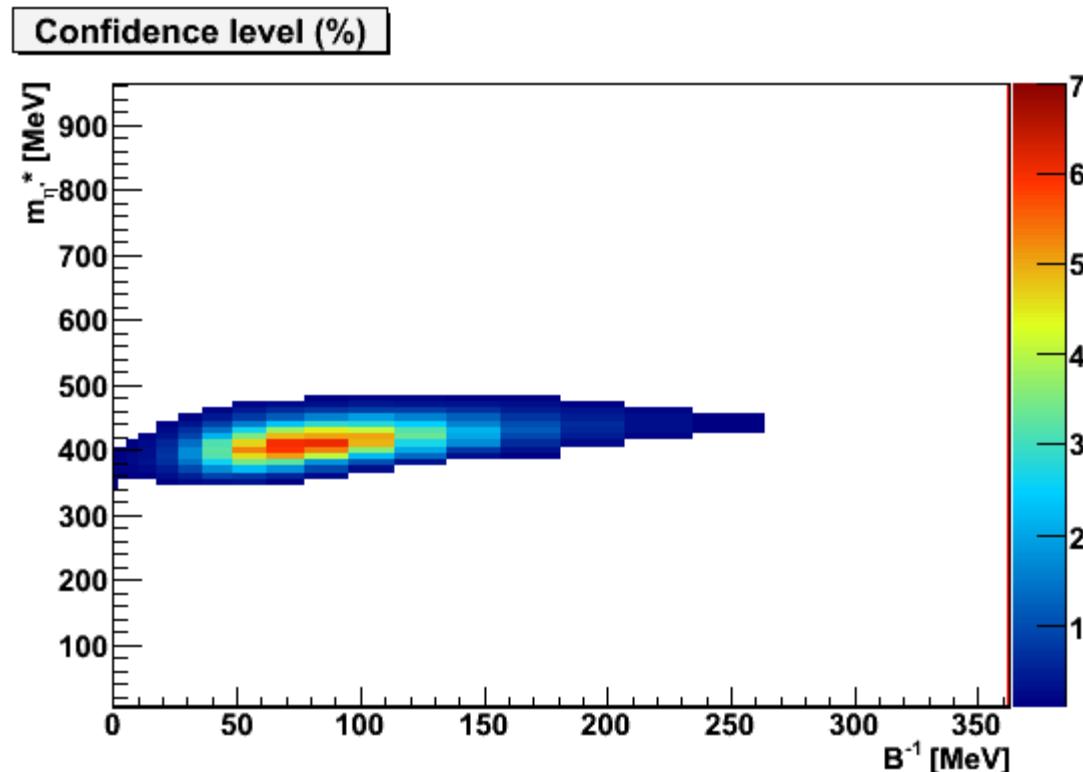
Confidence level (%)



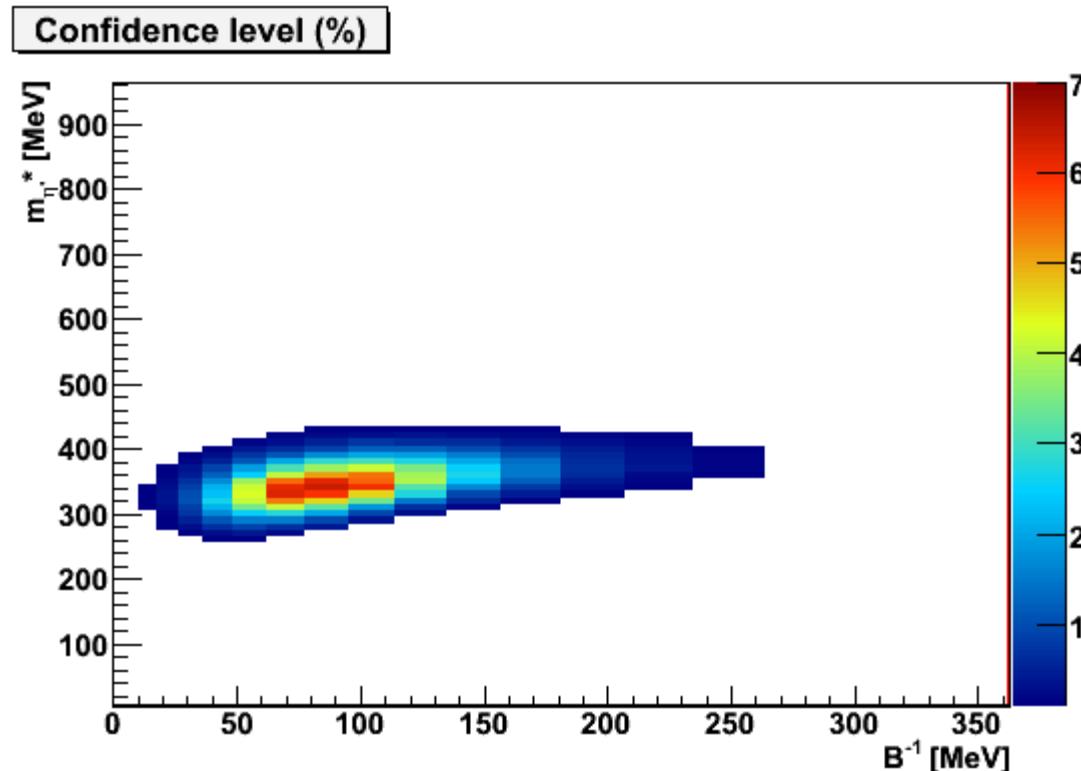
Rafelski vs. STAR



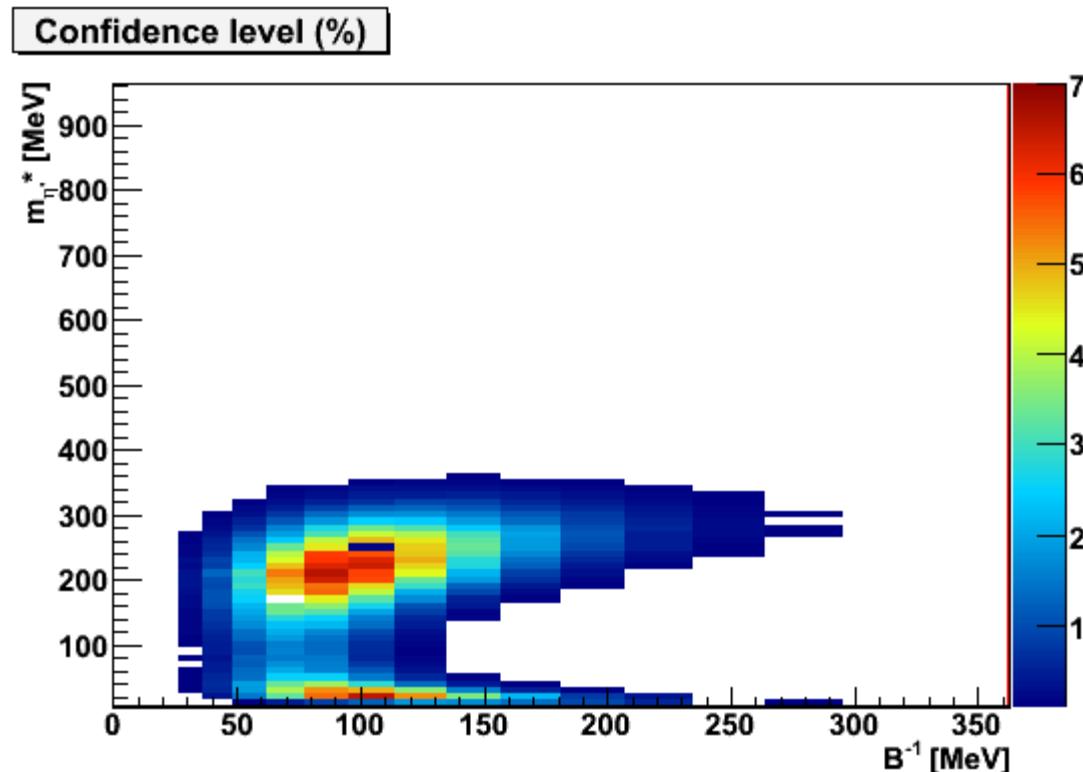
Systematics: Rafelski $\alpha=-1/2$



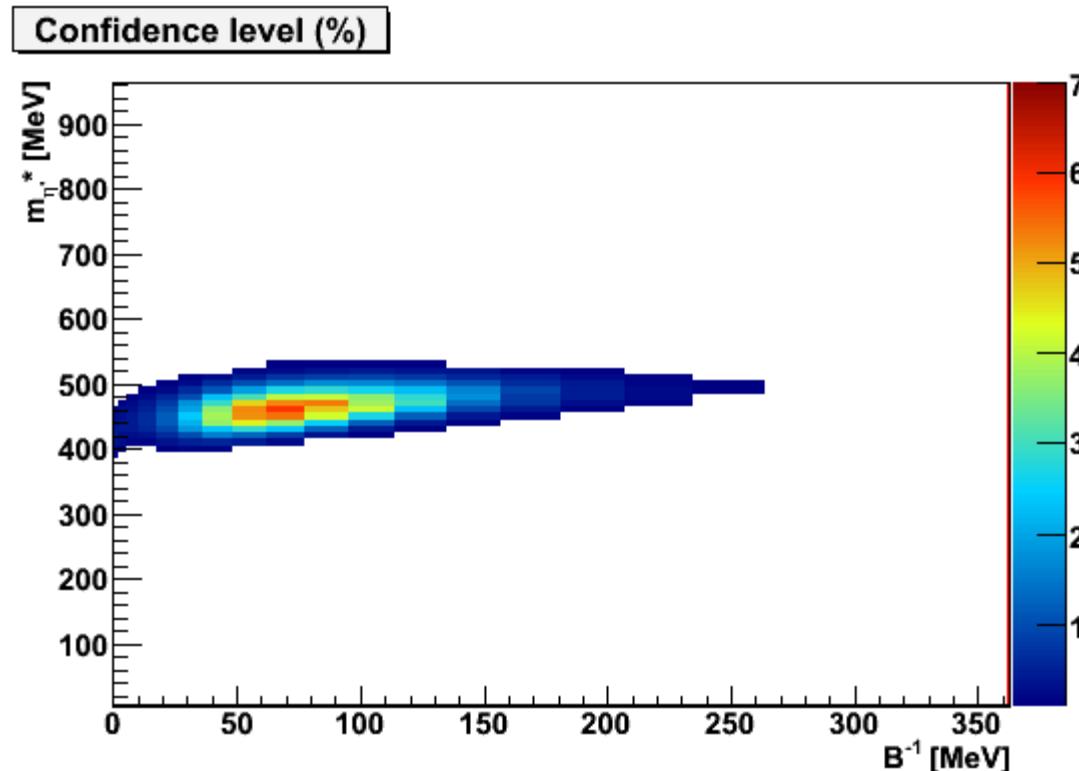
Systematics: Rafelski $\alpha=0$



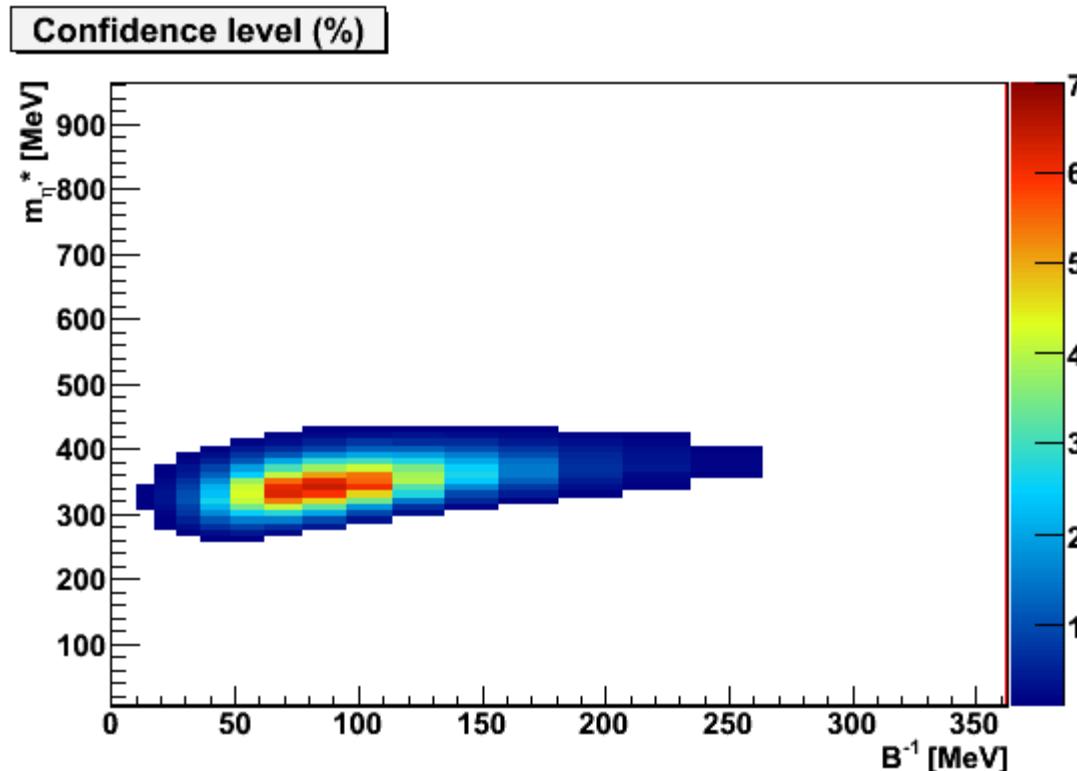
Systematics: Rafelski $\alpha=+1/2$



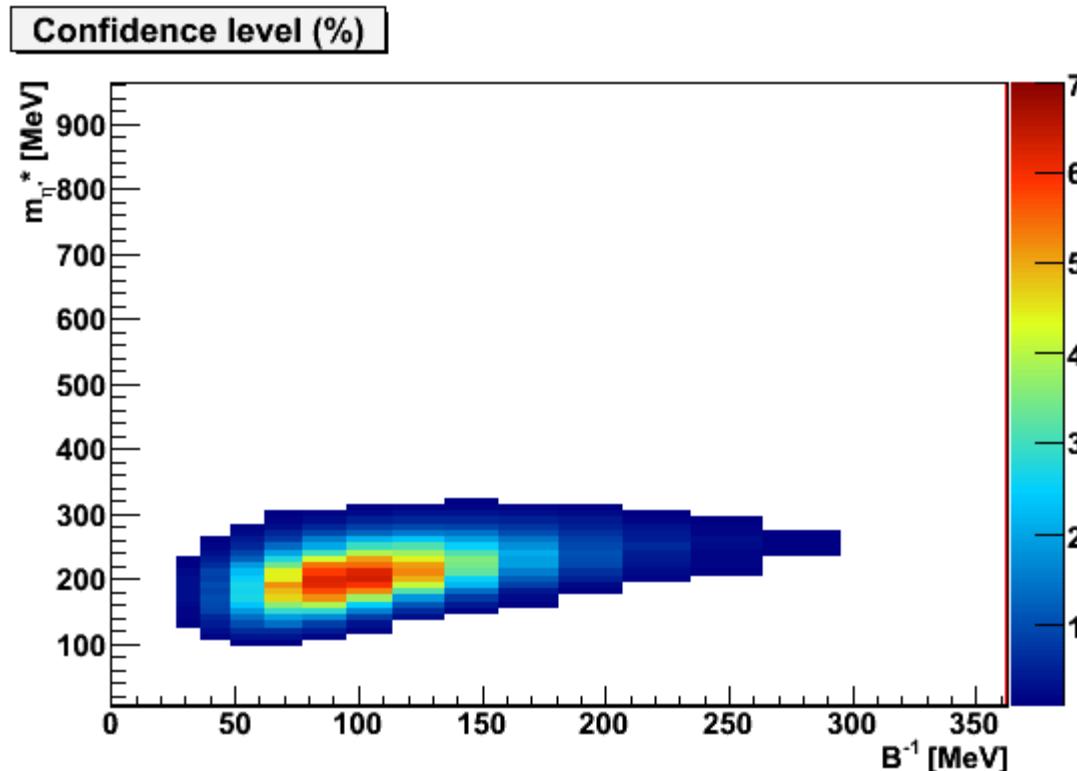
Systematics: Rafelski $T'=140$ MeV



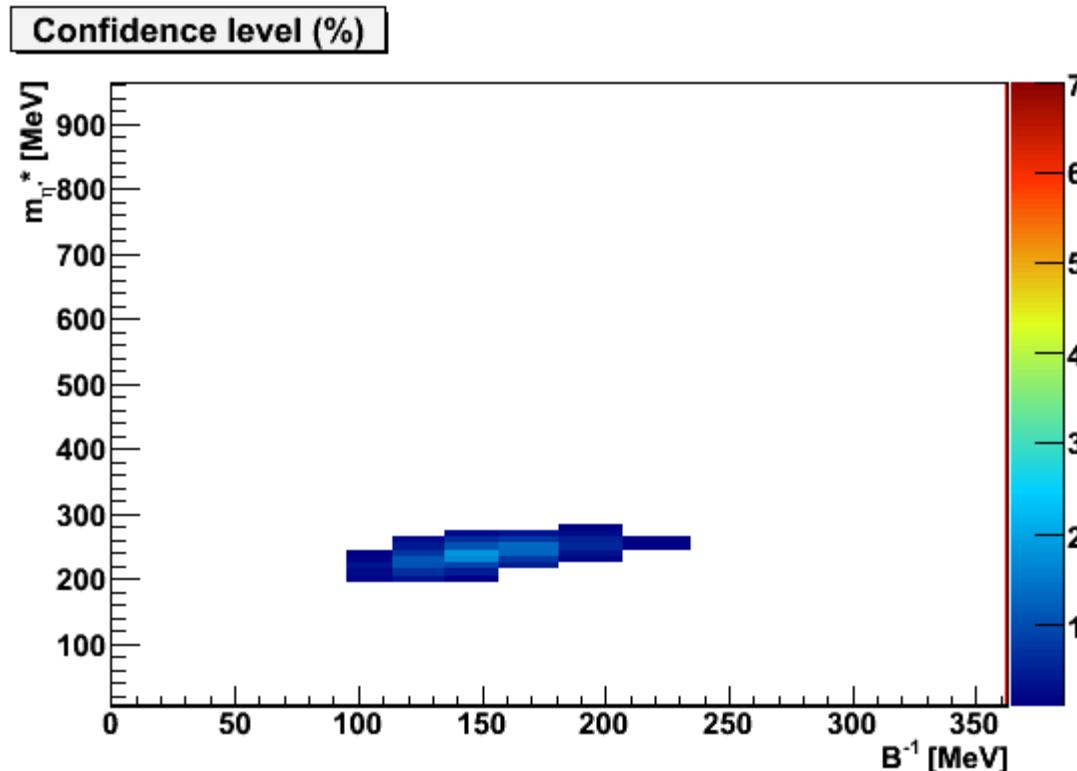
Systematics: Rafelski $T'=177$ MeV



Systematics: Rafelski $T'=220$ MeV



Systematics: Rafelski $T_{FO}=100$ MeV



Systematics: Rafelski $T_{FO}=177$ MeV

